

Academic Algebra 2
Pretest Matrices

KEY

1. Find the product of $\begin{bmatrix} -2 & -8 \\ -4 & 0 \\ 20 & 9 \end{bmatrix} \begin{bmatrix} 0 & 4 \\ -5 & 2 \end{bmatrix} =$

3×2 2×2
 3×2

$(-2)(0) + (-8)(-5)$ 40	$(-2)(4) + (-8)(2)$ $-8 + -16$ -24
$(-4)(0) + (0)(-5)$ 0	$(-4)(4) + (0)(2)$ -16
$(20)(0) + (9)(-5)$ -45	$(20)(4) + (9)(2)$ 98

2. Find the dimensions of the product of matrices

- A. 2×4 with a $4 \times 7 = \underline{2 \times 7}$
- B. 5×3 with a $5 \times 3 = \underline{\emptyset}$
- C. 6×2 with a $2 \times 1 = \underline{6 \times 1}$
- D. 2×1 with a $1 \times 2 = \underline{2 \times 2}$

3. Find n in the matrix equation, $4 \begin{bmatrix} -3 & 4 \\ n & 12 \end{bmatrix} + \begin{bmatrix} 0 & 6 \\ -5 & -15 \end{bmatrix} = \begin{bmatrix} -12 & 22 \\ -27 & 33 \end{bmatrix}$

$4n - 5 = -27$ $n = \frac{-22}{4} = \frac{-11}{2} = -5\frac{1}{2} = -5.5$

4. Find the inverse of $A = \begin{bmatrix} 6 & -3 \\ 8 & -2 \end{bmatrix}$, if it exists.

Switch CHANGE

$\begin{bmatrix} -2 & 6 \\ -8 & 3 \end{bmatrix}$ $\begin{bmatrix} -2 & 3 \\ -8 & 6 \end{bmatrix}$

$\frac{1}{\det}$ by det.
 $(6)(-2) - (8)(-3)$
 $-12 + 24$
12

So $A^{-1} = \begin{bmatrix} \frac{-2}{12} & \frac{3}{12} \\ \frac{-8}{12} & \frac{6}{12} \end{bmatrix} = \begin{bmatrix} \frac{-1}{6} & \frac{1}{4} \\ \frac{-2}{3} & \frac{1}{2} \end{bmatrix}$

5. Let $A = \begin{bmatrix} -8 & 1 \\ 4 & -5 \end{bmatrix}$ and $B = \begin{bmatrix} 6 & 4 \\ -7 & -1 \end{bmatrix}$. Find $A + 5B$.

$A = \begin{bmatrix} -8 & 1 \\ 4 & -5 \end{bmatrix}$ $5B = \begin{bmatrix} 30 & 20 \\ -35 & -5 \end{bmatrix} = \begin{bmatrix} 22 & 21 \\ -31 & -10 \end{bmatrix}$

6. Find $\begin{bmatrix} -15 & 7 \\ 72 & 8.6 \end{bmatrix} - \begin{bmatrix} -4 & -2 \\ 9 & 1 \end{bmatrix} = \begin{bmatrix} -15 - (-4) & 7 - (-2) \\ 72 - 9 & 8.6 - 1 \end{bmatrix} = \begin{bmatrix} -11 & 9 \\ 63 & 7.6 \end{bmatrix}$

7. Find the determinant of each 2 x 2 matrix:

$$\begin{bmatrix} 13 & 4 \\ -5 & -1 \end{bmatrix}$$

$$-13 - (-20)$$

$$7$$

$$\begin{bmatrix} 7 & 6 \\ 6 & 5 \end{bmatrix}$$

$$35 - 36$$

$$-1$$

$$\begin{bmatrix} \frac{1}{2} & 20 \\ \frac{3}{4} & 8 \end{bmatrix}$$

$$4 - \frac{3}{4} \cdot 20$$

$$4 - 15$$

$$-11$$

$$\begin{bmatrix} -10 & \frac{2}{5} \\ 35 & 15 \end{bmatrix}$$

$$-150 - 35(\frac{2}{5})$$

$$-150 - 14$$

$$-164$$

8. Find the product of $\begin{bmatrix} 3 & 1 \\ 5 & 2 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ -5 & 3 \end{bmatrix}$.

$$\begin{bmatrix} 6+5 & -3+3 \\ 10-10 & -5+6 \end{bmatrix} = \begin{bmatrix} 11 & 0 \\ 0 & 1 \end{bmatrix}$$

9. Find the values of w, x, y, and z that make the statement $\begin{bmatrix} 3x-5 & x+y \\ w^2-15 & \frac{4}{9}z \end{bmatrix} = \begin{bmatrix} 10 & 8 \\ 34 & 16 \end{bmatrix}$ true.

$$3x - 5 = 10$$

$$3x = 15$$

$$x = 5$$

$$x + y = 8$$

$$5 + y = 8$$

$$y = 3$$

$$w^2 - 15 = 34$$

$$\sqrt{w^2} = \sqrt{49}$$

$$w = 7, -7$$

$$\frac{4}{9}z = 16 \cdot \frac{9}{4}$$

$$z = 36$$

10. Solve the system of linear equations, $\begin{cases} 7m - 3n = 41 \\ 2m + 5n = 0 \end{cases}$ using Cramer's Rule.

$$(m) \quad x = \frac{D_x}{D} = \frac{\begin{vmatrix} 41 & -3 \\ 0 & 5 \end{vmatrix}}{\begin{vmatrix} 7 & -3 \\ 2 & 5 \end{vmatrix}} = \frac{205 - 0}{35 - 6} = \frac{205}{41} = 5 \quad (5, -2)$$

$$(n) \quad y = \frac{D_y}{D} = \frac{\begin{vmatrix} 7 & 41 \\ 2 & 0 \end{vmatrix}}{\begin{vmatrix} 7 & -3 \\ 2 & 5 \end{vmatrix}} = \frac{0 - 82}{35 - 6} = \frac{-82}{41} = -2$$

EQUATIONS REVIEW

11. Solve the absolute value equation $|3x + 5| = 9$

{Remember, to solve an absolute value equation, you write the equation TWICE...one positive, one negative}

$$|3x + 5| = 9$$

$$\begin{array}{r} 3x + 5 = 9 \\ -5 \quad -5 \\ \hline 3x = 4 \\ \boxed{x = \frac{4}{3}} \end{array}$$

$$\begin{array}{r} 3x + 5 = -9 \\ -5 \quad -5 \\ \hline 3x = -14 \\ \boxed{x = -\frac{14}{3}} \end{array}$$

12. Solve the equation: $7(4x - 5) + 20 = 19 - 8x + 11$

$$\begin{array}{r} 28x - 35 + 20 = 19 - 8x + 11 \\ 28x - 15 = 30 - 8x \\ + 8x \quad + 15 \quad + 15 \quad + 8x \\ \hline 36x = 45 \\ \boxed{x = \frac{45}{36} = \frac{5}{4}} \end{array}$$

13. Solve the equation: $\frac{3}{4}x + 44 = 62$

$$\begin{array}{r} \frac{3}{4}x + 44 = 62 \\ -44 \quad -44 \\ \hline \frac{3}{4}x = 18 \\ \cdot \frac{4}{3} \quad \cdot \frac{4}{3} \\ \hline \boxed{x = 24} \end{array}$$

$$\boxed{x = 24}$$

14. Solve the equation: $\frac{5}{2x+7} = \frac{9}{8-2x}$ {Hint: Cross Multiply}

$$\begin{array}{r} (5)(8-2x) = (9)(2x+7) \\ 40 - 10x = 18x + 63 \\ -63 + 10x \quad + 10x \quad - 63 \\ \hline -23 = 28x \\ \frac{-23}{28} = x \\ \boxed{x = -\frac{23}{28}} \end{array}$$

$$\boxed{x = -\frac{23}{28}}$$

Adding/Subtracting Decimals

Find each sum.

1) $5.4 + (-9.7)$

$$5.4 - 9.7$$

$$-4.3$$

$$\begin{array}{r} 9.7 \\ -5.4 \\ \hline 4.3 \end{array}$$

2) $10.8 + (-4.73)$

3) $(-0.5) + 0.3$

$$-0.2$$

4) $(-4.79) + (-0.4)$

5) $3.305 + 1.7$

$$1.7$$

$$5.005$$

6) $(-3.6) + 0.43$

7) $(-4.3) + 14.5$

$$\begin{array}{r} 14.5 \\ -4.3 \\ \hline 10.2 \end{array}$$

8) $(-7.1) + 3.63$

9) $13.7 + 3.2$

10) $(-10.9) + 6.1$

Find each difference.

11) $2.2 - 7.3$

12) $(-8.1) - (-8.9)$

13) $2.9 - 9.4$

14) $(-3.9) - 8.9$