

Chain Rule Practice

Doing derivatives with tables

x	f(x)	g(x)	f'(x)	g'(x)
3	1	8	-3	-5
6	3	-2	4	5
8	-1	3	π	4
1	2	-6	5	0

Find the derivative for each at $x = 3$

1. $f(x)g(x)$

$$f(x)g'(x) + g(x)f'(x)$$

$$1 \cdot -5 + 8 \cdot -3$$

$$\boxed{-29}$$

2. $\frac{f(x)}{g(x)}$

$$\frac{g f' - f g'}{g^2}$$

$$[8 \cdot -3 - 1 \cdot -5] / 64$$

$$\frac{-29}{64}$$

3. $\frac{g(x)}{f(x)} = \frac{f g' - g f'}{f^2}$

$$= \frac{3 \cdot 5 - 2 \cdot 2}{1 \cdot 5 - 8 \cdot -3}$$

$$= \frac{19}{1}$$

4. $(f(x))^2$

$$2 f(x) f'(x)$$

$$2 \cdot 1 \cdot -3$$

$$-6$$

5. $\sqrt{f(x)}$

$$\frac{f'}{2\sqrt{f}} = \frac{-3}{2\sqrt{1}} = -\frac{3}{2}$$

6. $\sqrt{f(x) + g(x)}$

$$\frac{f' + g'}{2\sqrt{f+g}} = \frac{-8}{2\sqrt{9}} = -\frac{4}{3}$$

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7. $\frac{1}{\sqrt[3]{g(x)}} = [g(x)]^{-\frac{1}{3}}$
 $-\frac{1}{3} [g(x)]^{-\frac{4}{3}} (g'(x))$
 $-\frac{1}{3} [g(3)]^{-\frac{4}{3}} (g'(3))$
 $-\frac{1}{3} (2^8)^{-\frac{4}{3}} (-5) = \frac{5}{248}$

9. $g(g(x))$
 $g'(g(x)) g'(x)$
 $g'(8) \cdot (-5)$
 $4 \cdot (-5)$
 -20

11. $f(2x)$
 $f'(2x)(2)$
 $f'(6)(2)$
 $4 \cdot 2$
 8

8. $\frac{f(x)}{f(x)+g(x)}$
 $\frac{[f(x)+g(x)]f'(x) - f(x)[f'(x)+g'(x)]}{[f(x)+g(x)]^2}$
 $\frac{9 \cdot (-3) - 1(-8)}{81} = \frac{-27+8}{81}$
 $-\frac{19}{81}$

10. $x^4 \sqrt{f(x)}$
 $x^4 \frac{1}{2\sqrt{f(x)}} f'(x) + \sqrt{f(x)} 4x^3$
 $\frac{81}{2} \frac{(-3)}{1} + 1 \cdot 4 \cdot 27$
 $-\frac{243}{2} + \frac{808}{1} = \frac{-27}{2}$

12. $[g(3x-1)]^3$
 $3[g(3x-1)]^2 g'(3x-1)(3)$
 $3[g(8)]^2 g'(8)(3)$
 $3(3)^2 4 \cdot 3 = 81 \cdot 4$
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